2026 **divides some** $222\cdots222$**.**

Submission deadline: November $28^{\textbf{th}}$ **2026**

Prove that there exists a positive multiple of 2026 whose decimal representation consists only of the digit 2.